



- $y_i = \alpha + b \text{ males}_i + e_i$
- $y_i = \alpha + b \text{ Females}_i + e_i$
- $y_i = b \text{ Males}_i + d \text{ Females}_i + e_i$

4 North east (= location)

location = $\begin{cases} 1, & \text{South} \\ 2, & \text{Midwest} \\ 3, & \text{West} \\ 4 & \text{North east} \end{cases}$ ←

South_i = $\begin{cases} 1, & A \sim \text{Kadonkai South} \\ 0, & A \sim \text{SFU Kadonkai South} \end{cases}$

Midwest_i = $\begin{cases} 1, & A \sim \text{Kadonkai Midwest} \\ 0, & A \sim \text{SFU Kadonkai Midwest} \end{cases}$

West_i = $\begin{cases} 1 & A \sim \text{Kadonkai West} \\ 0 & A \sim \text{SFU Kadonkai West} \end{cases}$

$$\text{wage}_i = \alpha + \beta \text{edu}_i + \gamma \text{South}_i + \delta \text{Midwest}_i + \theta \text{West}_i + \epsilon_i$$

$$\hat{\beta} = 1.11, \quad \hat{\gamma} = -1.55, \quad \hat{\delta} = -0.42, \quad \hat{\theta} = -0.56$$

$$E(\text{wage}_i | \text{edu}_i) = \begin{cases} \alpha + \beta \text{edu}_i, & \text{North East} \\ (\alpha + \gamma) + \beta \text{edu}_i, & \text{South} \\ (\alpha + \delta) + \beta \text{edu}_i, & \text{Midwest} \\ (\alpha + \theta) + \beta \text{edu}_i, & \text{West} \end{cases}$$

$$\frac{\partial E(\text{wage}_i)}{\partial \text{edu}_i} = \beta$$

$$\begin{aligned} d &= [\alpha + \gamma + \beta \text{edu}_i^S] - [\alpha + \beta \text{edu}_i^N] \\ &= \gamma + \beta (\text{edu}_i^S - \text{edu}_i^N) \\ &\quad \underbrace{\hspace{10em}}_{=0} \end{aligned}$$