

Finance for Cultural Organisations
Lecture 6. Stock Valuation

## Lecture 6: Stock Valuation

- Understand how stock prices depend on future dividends and dividend growth
- Be able to compute stock prices using the dividend growth model
- Understand how corporate directors are elected
- Understand how stock markets work
- Understand how stock prices are quoted

Reading

- RWJ Ch8, HBP Ch5,6.


## Cash Flows for Stockholders

- If you buy a share of stock, you can receive cash in two ways
- The company pays dividends
- You sell your shares, either to another investor in the market or back to the company
- As with bonds, the price of the stock is the present value of these expected cash flows


## One-Period Example

- Suppose you are thinking of purchasing the stock of Moore Oil, Inc. and you expect it to pay a $\$ 2$ dividend in one year and you believe that you can sell the stock for $\$ 14$ at that time. If you require a return of $20 \%$ on investments of this risk, what is the maximum you would be willing to pay?
- Compute the PV of the expected cash flows
- Price $=(14+2) /(1.2)=\$ 13.33$
- Or FV = 16; $\mathrm{I} / \mathrm{Y}=20 ; \mathrm{N}=1 ; \mathrm{CPT}$ PV $=-13.33$


## Two-Period Example

- Now what if you decide to hold the stock for two years? In addition to the dividend in one year, you expect a dividend of $\$ 2.10$ in two years and a stock price of $\$ 14.70$ at the end of year 2. Now how much would you be willing to pay?
$-P V=2 /(1.2)+(2.10+14.70) /(1.2)^{2}=13.33$


## Three-Period Example

- Finally, what if you decide to hold the stock for three years? In addition to the dividends at the end of years 1 and 2, you expect to receive a dividend of $\$ 2.205$ at the end of year 3 and the stock price is expected to be $\$ 15.435$. Now how much would you be willing to pay?
$-P V=2 / 1.2+2.10 /(1.2)^{2}+(2.205+15.435) /(1.2)^{3}=$ 13.33


## Developing The Model

- You could continue to push back the year in which you will sell the stock
- You would find that the price of the stock is really just the present value of all expected future dividends
- So, how can we estimate all future dividend payments?


## Estimating Dividends: Special Cases

- Constant dividend
- The firm will pay a constant dividend forever
- This is like preferred stock
- The price is computed using the perpetuity formula
- Constant dividend growth
- The firm will increase the dividend by a constant percent every period
- Supernormal growth
- Dividend growth is not consistent initially, but settles down to constant growth eventually


## Zero Growth

- If dividends are expected at regular intervals forever, then this is a perpetuity and the present value of expected future dividends can be found using the perpetuity formula

$$
-P_{0}=D / R
$$

- Suppose stock is expected to pay a $\$ 0.50$ dividend every quarter and the required return is $10 \%$ with quarterly compounding. What is the price?
$-P_{0}=.50 /(.1 / 4)=\$ 20$


## Dividend Growth Model

- Dividends are expected to grow at a constant percent per period.
$-P_{0}=D_{1} /(1+R)+D_{2} /(1+R)^{2}+D_{3} /(1+R)^{3}+\ldots$
$-\mathrm{P}_{0}=\mathrm{D}_{0}(1+\mathrm{g}) /(1+\mathrm{R})+\mathrm{D}_{0}(1+\mathrm{g})^{2} /(1+\mathrm{R})^{2}+\mathrm{D}_{0}(1+\mathrm{g})^{3} /(1+\mathrm{R})^{3}+\ldots$
- With a little algebra and some series work, this reduces to:

$$
P_{0}=\frac{D_{0}(1+g)}{R-g}=\frac{D_{1}}{R-g}
$$

## DGM - Example 1

- Suppose Big D, Inc. just paid a dividend of $\$ .50$. It is expected to increase its dividend by $2 \%$ per year. If the market requires a return of $15 \%$ on assets of this risk, how much should the stock be selling for?
- $\mathrm{P}_{0}=.50(1+.02) /(.15-.02)=\$ 3.92$


## DGM - Example 2

- Suppose TB Pirates, Inc. is expected to pay a $\$ 2$ dividend in one year. If the dividend is expected to grow at 5\% per year and the required return is $20 \%$, what is the price?
$-P_{0}=2 /(.2-.05)=\$ 13.33$
- Why isn't the $\$ 2$ in the numerator multiplied by (1.05) in this example?


## Stock Price Sensitivity to Dividend Growth, g



## Stock Price Sensitivity to Required Return, R



## Example Gordon Growth Company - I

- Gordon Growth Company is expected to pay a dividend of $\$ 4$ next period and dividends are expected to grow at $6 \%$ per year. The required return is $16 \%$.
- What is the current price?
$-P_{0}=4 /(.16-.06)=\$ 40$
- Remember that we already have the dividend expected next year, so we don't multiply the dividend by $1+g$


## Example Gordon Growth Company - II

- What is the price expected to be in year 4?

$$
\begin{aligned}
& -P_{4}=D_{4}(1+g) /(R-g)=D_{5} /(R-g) \\
& -P_{4}=4(1+.06)^{4} /(.16-.06)=50.50
\end{aligned}
$$

- What is the implied return given the change in price during the four year period?
$-50.50=40(1+\text { return })^{4}$; return $=6 \%$
$-\mathrm{PV}=-40 ; \mathrm{FV}=50.50 ; \mathrm{N}=4 ; \mathrm{CPT} \mathrm{I} / \mathrm{Y}=6 \%$
- The price grows at the same rate as the dividends


## Nonconstant Growth Problem Statement

- Suppose a firm is expected to increase dividends by $20 \%$ in one year and by $15 \%$ in two years. After that dividends will increase at a rate of $5 \%$ per year indefinitely. If the last dividend was $\$ 1$ and the required return is $20 \%$, what is the price of the stock?
- Remember that we have to find the PV of all expected future dividends.


## Nonconstant Growth - Example Solution

- Compute the dividends until growth levels off
$-D_{1}=1(1.2)=\$ 1.20$
$-D_{2}=1.20(1.15)=\$ 1.38$
$-D_{3}=1.38(1.05)=\$ 1.449$
- Find the expected future price

$$
-P_{2}=D_{3} /(R-g)=1.449 /(.2-.05)=9.66
$$

- Find the present value of the expected future cash flows

$$
-P_{0}=1.20 /(1.2)+(1.38+9.66) /(1.2)^{2}=8.67
$$

## Quick Quiz - Part I

- What is the value of a stock that is expected to pay a constant dividend of $\$ 2$ per year if the required return is $15 \%$ ?
- What if the company starts increasing dividends by 3\% per year, beginning with the next dividend? The required return stays at $15 \%$.


## Using the DGM to Find R

- Start with the DGM:

$$
\begin{aligned}
& P_{0}=\frac{D_{0}(1+g)}{R-g}=\frac{D_{1}}{R-g} \\
& \text { rearrange and solve for } R
\end{aligned}
$$

$$
R=\frac{D_{0}(1+g)}{P_{0}}+g=\frac{D_{1}}{P_{0}}+g
$$

## Finding the Required Return - Example

- Suppose a firm's stock is selling for $\$ 10.50$. They just paid a \$1 dividend and dividends are expected to grow at 5\% per year. What is the required return?
$-R=[1(1.05) / 10.50]+.05=15 \%$
- What is the dividend yield?
- 1(1.05) / $10.50=10 \%$
- What is the capital gains yield?
$-\mathrm{g}=5 \%$


## I. The General Case

In general, the price today of a share of stock, $P_{0}$, is the present value of all of its future dividends, $D_{1}, D_{2}, D_{3} \ldots$ :

$$
P_{0}=\frac{D_{1}}{(1+R)^{1}}+\frac{D_{2}}{(1+R)^{2}}+\frac{D_{3}}{(1+R)^{3}}+\cdots
$$

where $R$ is the required return.

## II. Constant Growth Case

If the dividend grows at a steady rate, $g$, then the price can be written as:

$$
P_{0}=\frac{D_{1}}{R-g}
$$

## Summary

of
Stock
Valuation

This result is called the dividend growth model.

## III. Supernormal Growth

If the dividend grows steadily after $t$ periods, then the price can be written as:

$$
P_{0}=\frac{D_{1}}{(1+R)^{1}}+\frac{D_{2}}{(1+R)^{2}}+\cdots+\frac{D_{t}}{(1+R)^{t}}+\frac{P_{t}}{(1+R)^{t}}
$$

where

$$
P_{\mathrm{t}}=\frac{D_{\mathrm{t}} \times(1+g)}{(R-g)}
$$

## IV. The Required Return

The required return, $R$, can be written as the sum of two things:

$$
R=D_{1} / P_{0}+g
$$

where $D_{1} / P_{0}$ is the dividend yield and $g$ is the capital gains yield (which is the same thing as the growth rate in dividends for the steady growth case).

## Features of Common Stock

- Voting Rights
- Proxy voting
- Classes of stock
- Other Rights
- Share proportionally in declared dividends
- Share proportionally in remaining assets during liquidation
- Preemptive right - first shot at new stock issue to maintain proportional ownership if desired


## Dividend Characteristics

- Dividends are not a liability of the firm until a dividend has been declared by the Board
- Consequently, a firm cannot go bankrupt for not declaring dividends
- Dividends and Taxes
- Dividend payments are not considered a business expense; therefore, they are not tax deductible
- The taxation of dividends received by individuals depends on the holding period
- Dividends received by corporations have a minimum 70\% exclusion from taxable income


## Features of Preferred Stock

- Dividends
- Stated dividend that must be paid before dividends can be paid to common stockholders
- Dividends are not a liability of the firm and preferred dividends can be deferred indefinitely
- Most preferred dividends are cumulative - any missed preferred dividends have to be paid before common dividends can be paid
- Preferred stock generally does not carry voting rights


## Stock Market

- Dealers vs. Brokers
- New York Stock Exchange (NYSE)
- Largest stock market in the world
- Members
- Own seats on the exchange
- Commission brokers
- Specialists
- Floor brokers
- Floor traders
- Operations
- Floor activity


## NASDAQ

- Not a physical exchange - computer-based quotation system
- Multiple market makers
- Electronic Communications Networks
- Three levels of information
- Level 1 - median quotes, registered representatives
- Level 2 - view quotes, brokers \& dealers
- Level 3 - view and update quotes, dealers only
- Large portion of technology stocks

Quick Quiz - Part II

- You observe a stock price of $\$ 18.75$. You expect a dividend growth rate of $5 \%$ and the most recent dividend was $\$ 1.50$. What is the required return?
- What are some of the major characteristics of common stock?
- What are some of the major characteristics of preferred stock?


## Comprehensive Problem

- XYZ stock currently sells for $\$ 50$ per share. The next expected annual dividend is $\$ 2$, and the growth rate is $6 \%$. What is the expected rate of return on this stock?
- If the required rate of return on this stock were $12 \%$, what would the stock price be, and what would the dividend yield be?

