

# LZ77 – Exercise

Multimedia Technology

Tutorial 2, section 2a

# LZ77

Assume we are applying LZ77 encoding with a 4+4 character window, starting with the left part of the window empty.

Show how the sequence "aababbbbbbbb" is encoded and how the output from the encoder is decoded.

aaba bbbbbbb

In each step, we need to:

- Select as **input** from the right window the maximum number of symbols that we can match in the left window.
- Extract the code (o,l,c)  
where **o** is the index of the left position,  
where **l** (L lowercase) is the length of the matched string,  
and **c** is the next symbol we did not match.
- In the next step we slide to the right by the number of symbols matched (n+1)

Step 1

aabaabbbb

0	1	2	3
---	---	---	---

				a	a	b	a
--	--	--	--	---	---	---	---

The initial window is empty (4 empty cells).

Input: a

Step 1

aaba bbbbbb

0	1	2	3
---	---	---	---

				a	a	b	a
--	--	--	--	---	---	---	---

The initial window is empty (4 empty cells).

Input: a

Code: (0,0,a)

We don't have a  
match

Step 2

aababbbbbbb

0	1	2	3
---	---	---	---

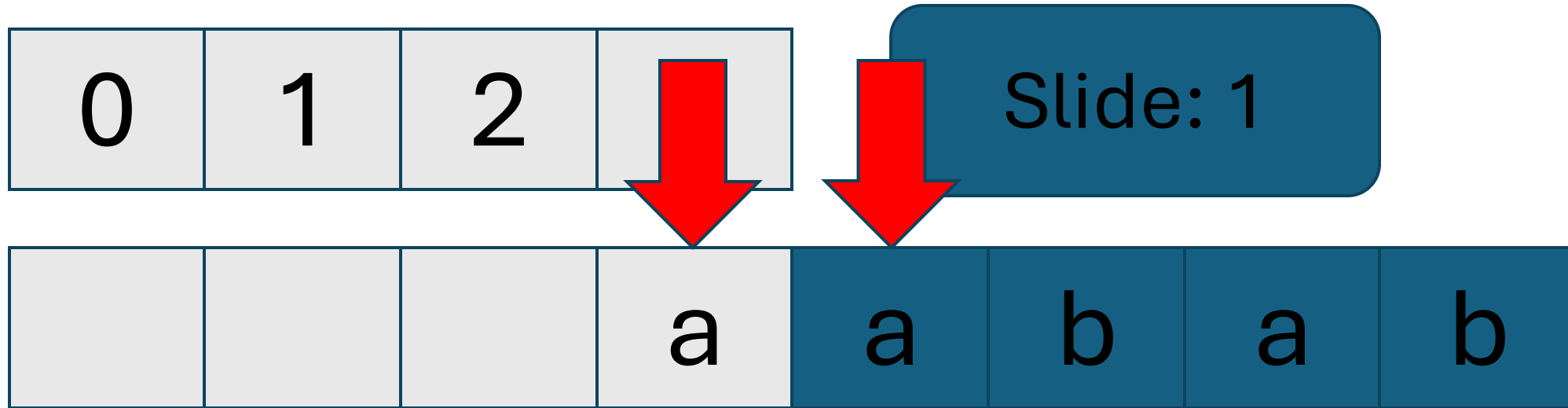
Slide: 1

			a	a	b	a	b
--	--	--	---	---	---	---	---

Input:  
ab

Step 2

aababbbbbbb



Slide: 1

Input:  
ab

Code: (3,1,b)

We matched the 'a' (1st on the right) with the 'a' at position 3 (from the left).

Step 3

aababbbbbb

0	1	2	3
---	---	---	---

Slide: 2

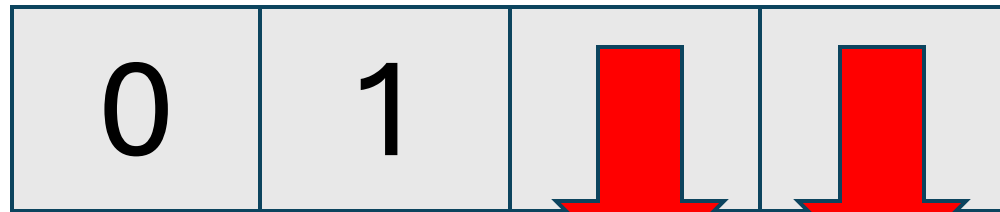
	a	a	b	a	b	b	b
--	---	---	---	---	---	---	---

Input: abb



Step 3

aababbbbbb



Slide: 2

Input: abb

Code: (2,2,b)

We matched ab with ab at position 2(from the left)

Step 4

aab**aab**bbbb

0	1	2	3
---	---	---	---

Slide: 3

b	a	b	b	b	b	b	b
---	---	---	---	---	---	---	---

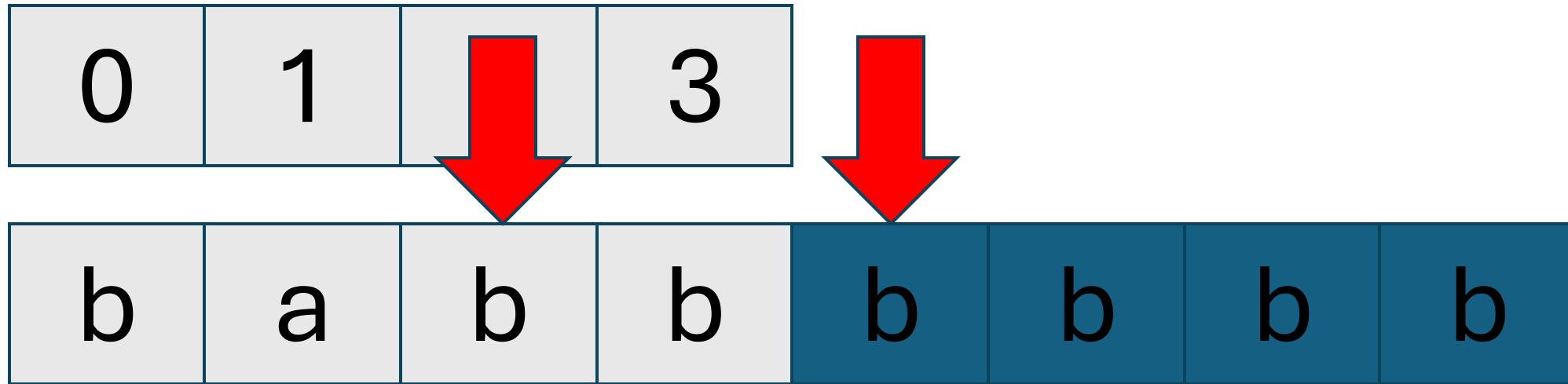
Input: bbbb

Code: (2,3,b)

We matched 3 'b' from the right with 3 'b' from the left

Step 4

aab**aa****bbbbb**



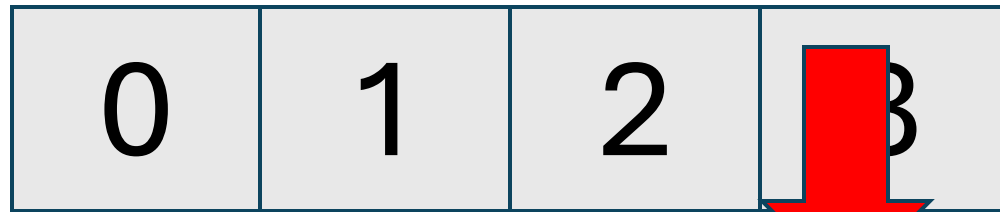
Input: bbbb

Code: (2,3,b)

We matched 3 'b' from the right with 3 'b' from the left

Step 4

aab**aab**bbbb

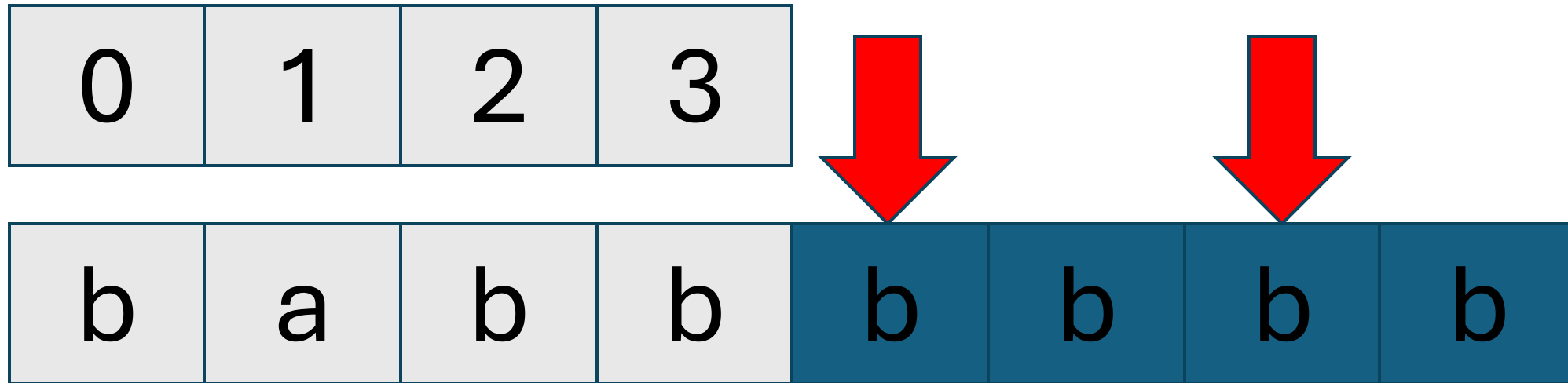


Input: bbbb

Code: (2,3,b)

We matched 3 'b' from the right with 3 'b' from the left

aab**aab**bbbb



Code: (2,3,b)

We matched 3 'b' from the right with 3 'b' from the left

Decoding the output from the encoder.

Step 1

0	1	2	3
---	---	---	---

				?	?	?	?
--	--	--	--	---	---	---	---

Code: (0,0,a)

Step 1

0	1	2	3
---	---	---	---

Slide: 1

			a	?	?	?	?
--	--	--	---	---	---	---	---

Code: (0,0,a)

Output: a



Step 2

0	1	2	3
---	---	---	---

			a	?	?	?	?
--	--	--	---	---	---	---	---

Code: (3,1,b)

## Step 2

0	1	2	3
---	---	---	---

Slide: 2

	a	a	b	?	?	?	?
--	---	---	---	---	---	---	---

Code: (3,1,b)

Output: ab

## Step 3

0	1	2	3
---	---	---	---

	a	a	b	?	?	?	?
--	---	---	---	---	---	---	---

Code: (2,2,b)

## Step 3

0	1	2	3
---	---	---	---

	a	a	b	?	?	?	?
--	---	---	---	---	---	---	---

Code: (2,2,b)

Output: abb

Step 4

0	1	2	3
---	---	---	---

Slide: 3

b	a	b	b	?	?	?	?
---	---	---	---	---	---	---	---

Code: (2,2,b)

Output: abb

## Step 4

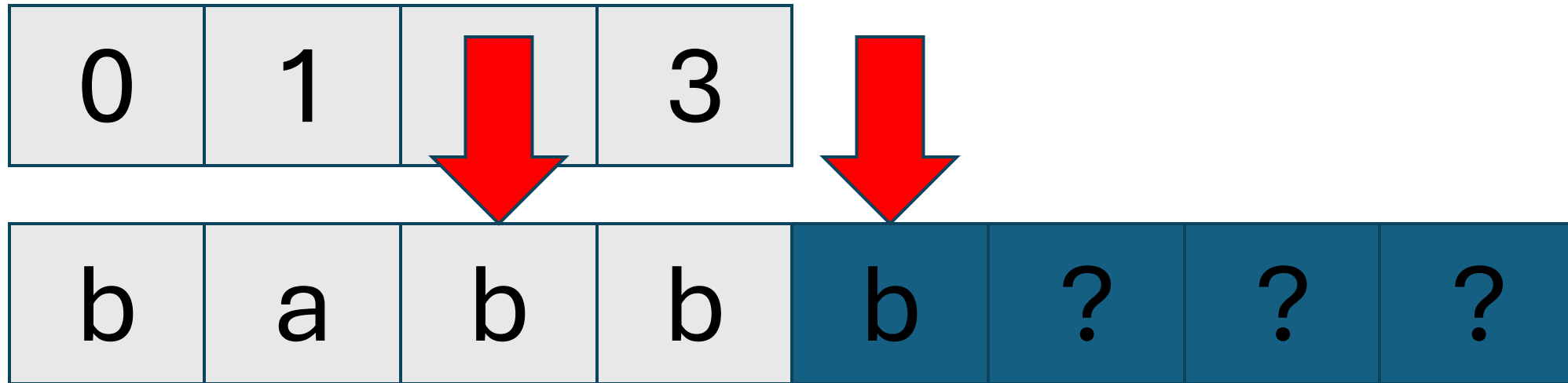
0	1	2	3
---	---	---	---

b	a	b	b	?	?	?	?
---	---	---	---	---	---	---	---

Code: (2,3,b)

I have to copy 3 'b's from  
position 2 onwards

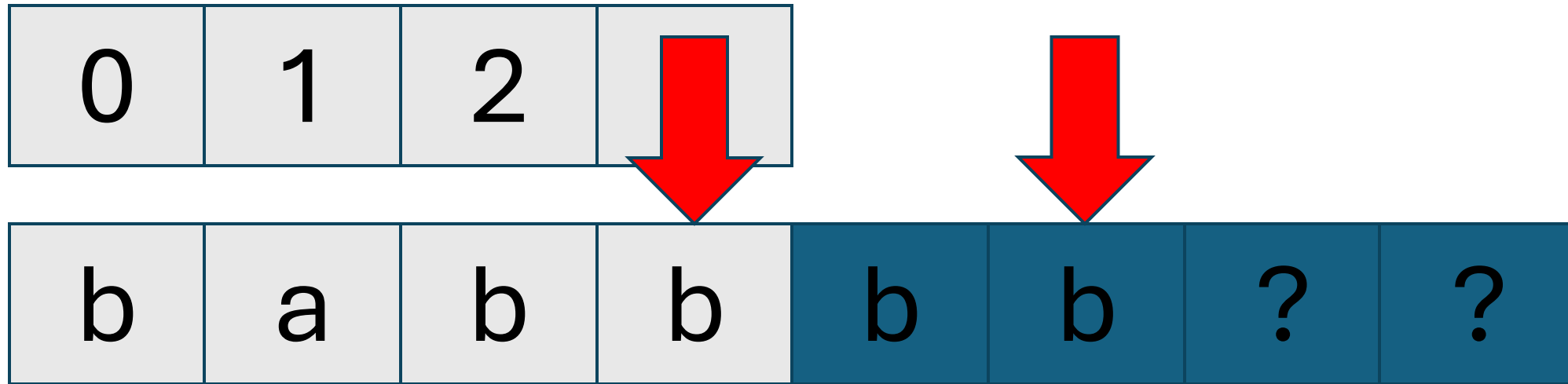
## Step 5



Code: (2,3,b)

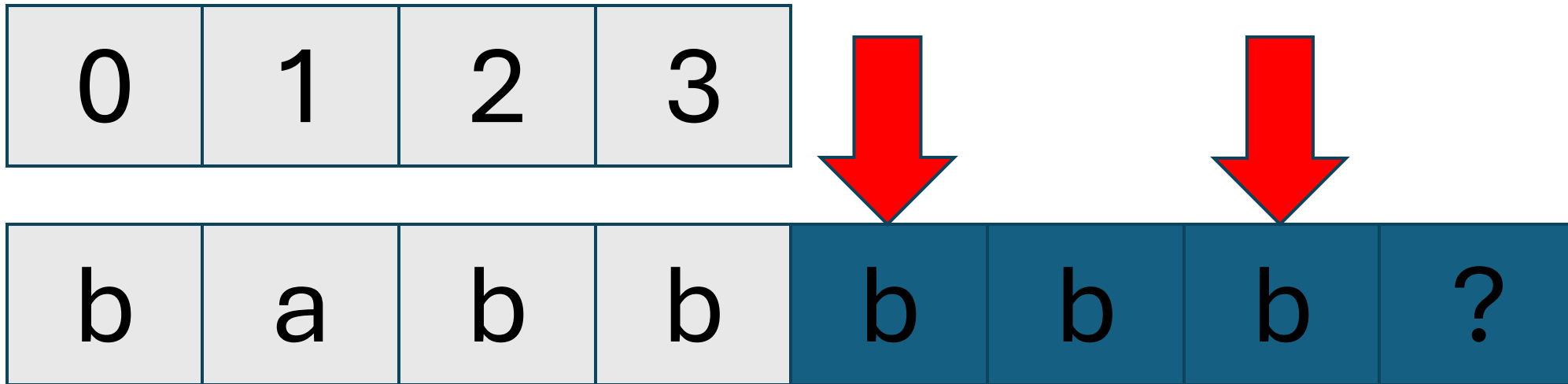
1<sup>st</sup> b

## Step 5





## Step 5



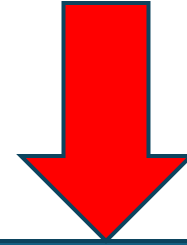
Code: (2,3,b)

3<sup>rd</sup> b

## Step 6

0	1	2	3
---	---	---	---

b	a	b	b	b	b	b	b
---	---	---	---	---	---	---	---



Code: (2,3,b)

I add the final b (the symbol that I know from the code wasn't matched)