

Arithmetic Coding

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Exercise - encoding

Multimedia Technology

Tutorial 2, section 1a

Arithmetic Coding

An information source produces the symbols A, B, C and \$ (terminal symbol).

Construct the interval table and encode the string AABC\$ with a decimal number using arithmetic coding (calculate the probabilities from the string).

Calculate the probabilities from the string: AABC\$

In the given string AABC\$, we have 5 symbols, and A appears twice, thus $A = 0.4$.

Similarly for the rest of the symbols we have the following probabilities:

$$A = 0.4 \implies A: [0, 0.4)$$

$$B = 0.2 \implies B: [0.4, 0.6)$$

$$C = 0.2 \implies C: [0.6, 0.8)$$

$$\$ = 0.2 \implies \$: [0.8, 1)$$

min and max

A: [0 , 0.4)

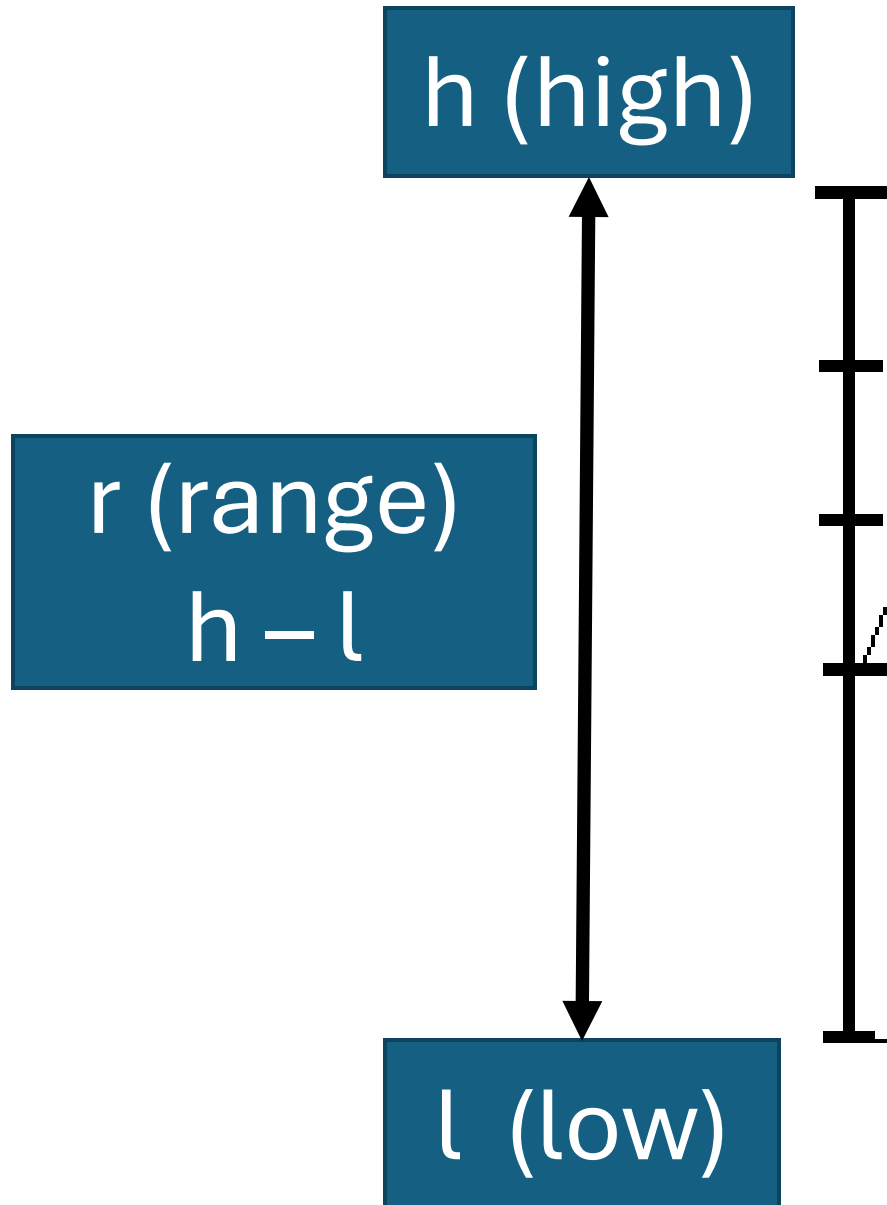
min

max

min: start point of the interval assigned to the symbol based on its probability

max: end point of the interval assigned to the symbol based on its probability

high, low, range



low and high: current bounds of the interval that represents the encoded message up to the current symbol

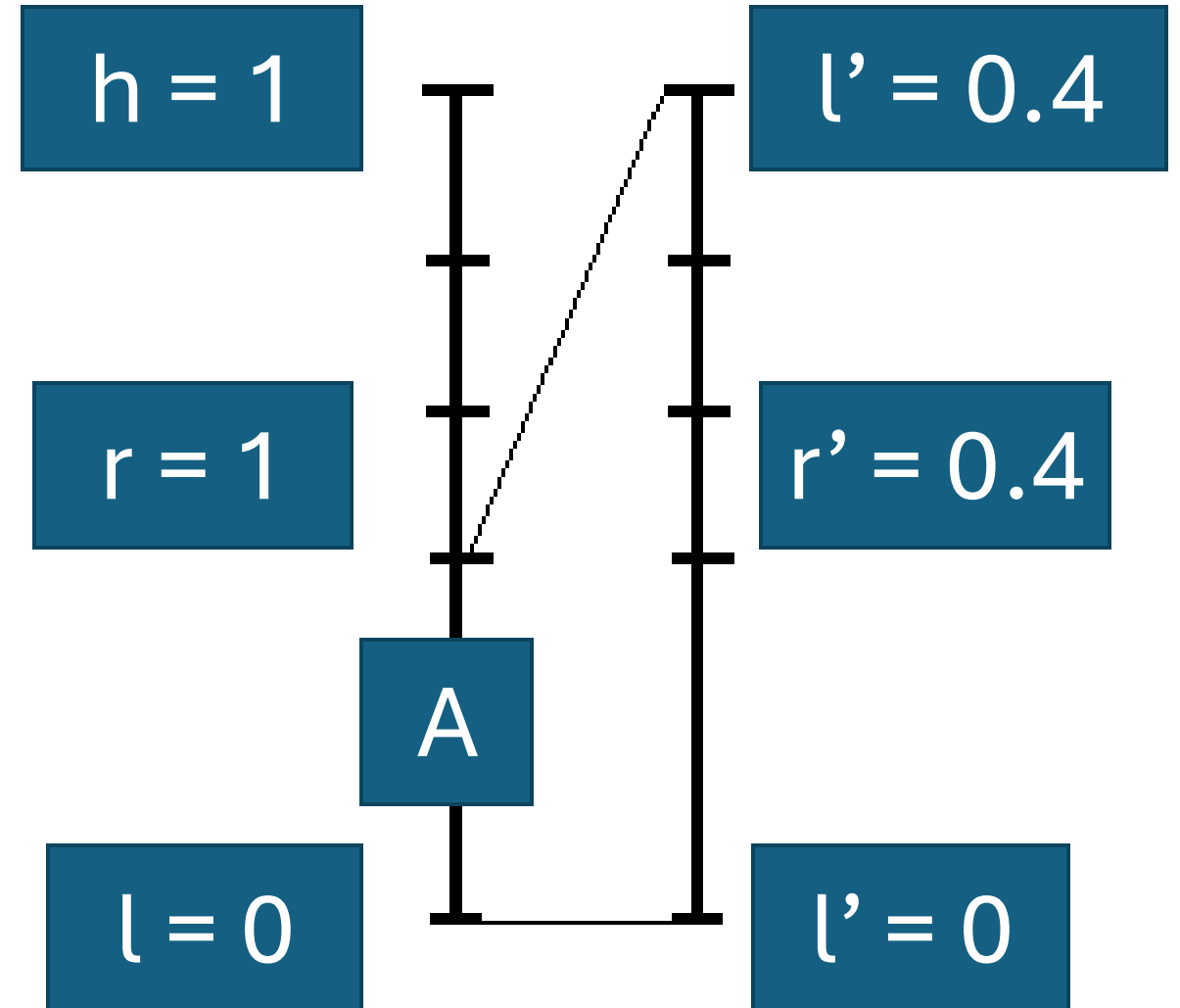
range: width of current interval before refining it with the next symbol

- We encode the string AABC\$ by refining the range for each symbol sequentially.

A

$$h' = l + r * \max$$
$$l' = l + r * \min$$

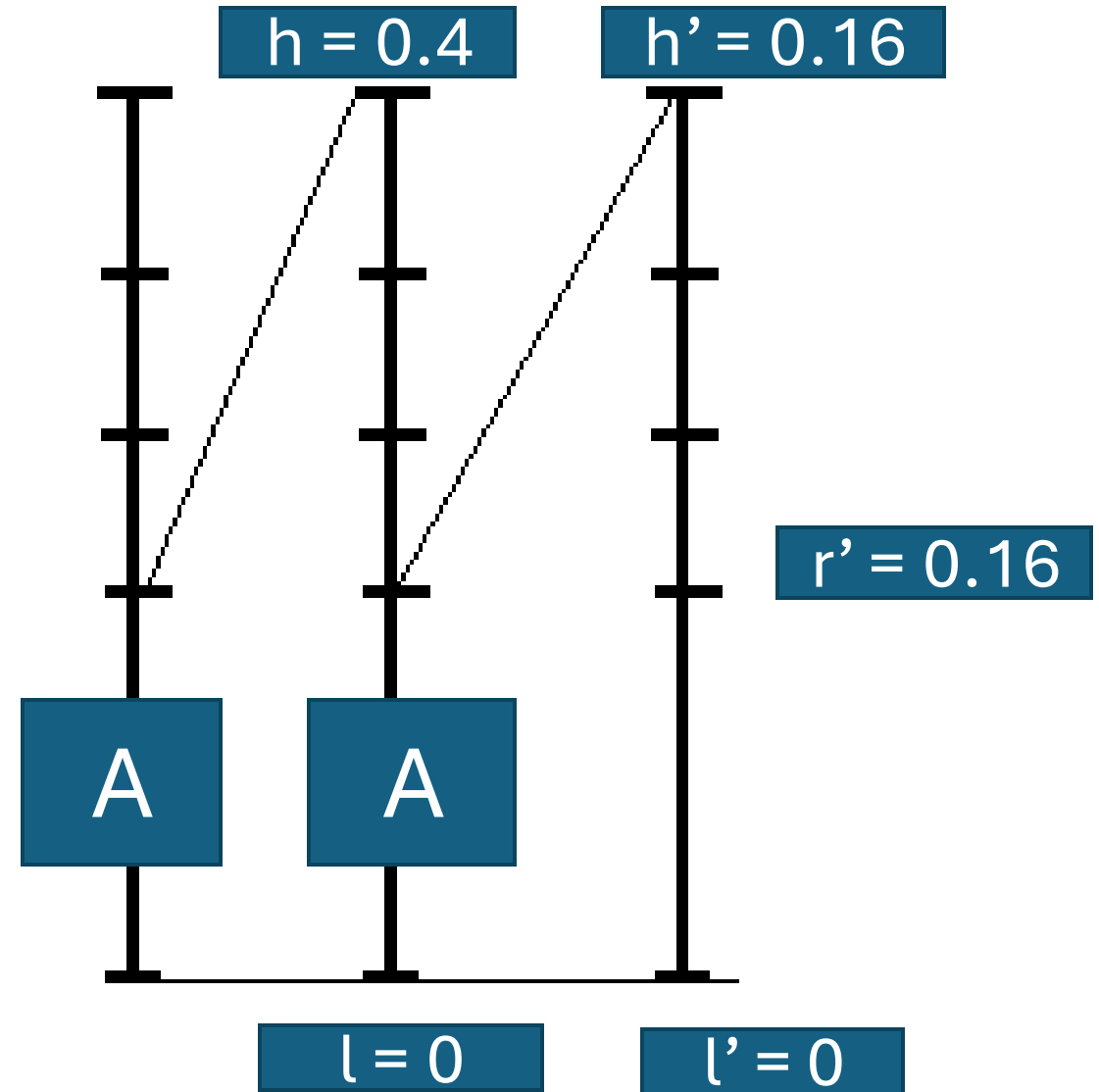
- $h = 1$
- $l = 0$
- $r = 1$ (range)
- $h' = 0 + 1 * 0.4 = 0.4$
- $l' = 0 + 1 * 0 = 0$
- $r' = H' - L' = 0.4 - 0 = 0.4$



A

$$h' = l + r * \max$$
$$l' = l + r * \min$$

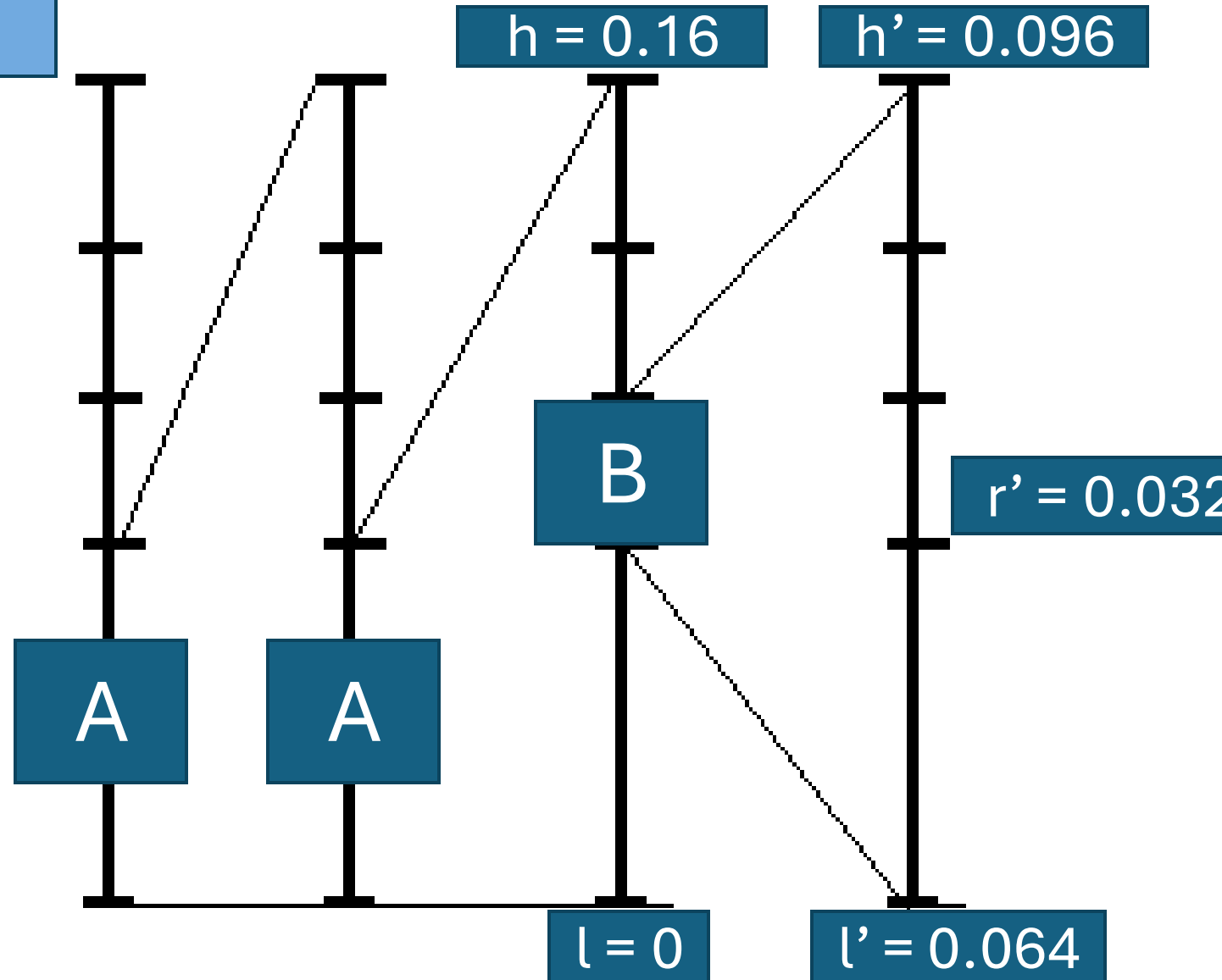
- $h = 0.4$
- $l = 0$
- $r = 0.4$
- $h' = 0 + 0.4 * 0.4 = 0.16$
- $l' = 0 + 0.4 * 0 = 0$
- $r' = h' - l' = 0.16 - 0 = 0.16$



B

$$h' = l + r * \max$$
$$l' = l + r * \min$$

- $h = 0.16$
- $l = 0$
- $r = 0.16$
- $h' = 0 + 0.16 * 0.6 = 0.096$
- $l' = 0 + 0.16 * 0.4 = 0.064$
- $r' = h' - l' = 0.096 - 0.064 = 0.032$

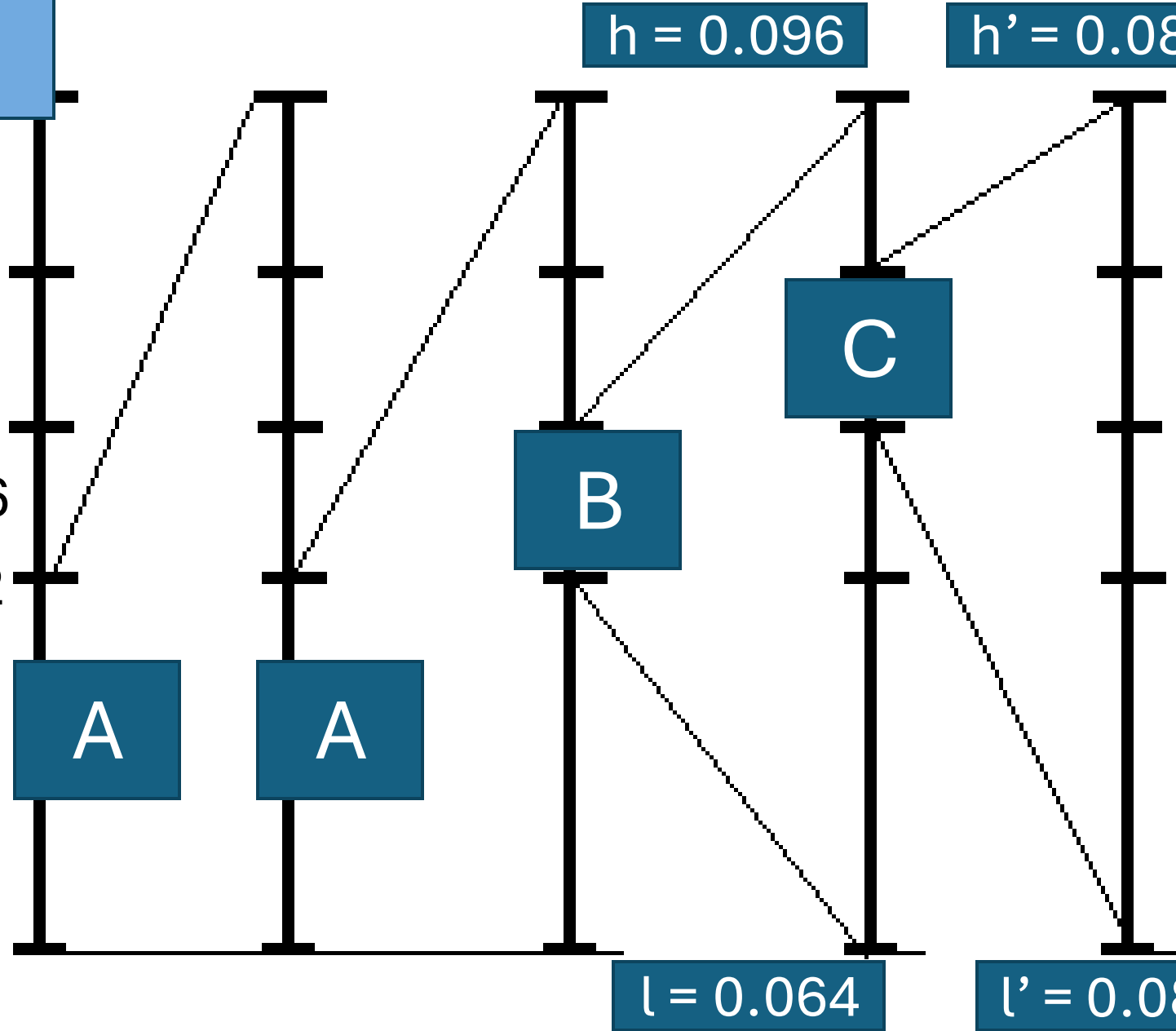


C

$$h' = l + r * \max$$

$$l' = l + r * \min$$

- $h = 0.096$
- $l = 0.064$
- $r = 0.032$
- $h' = 0.064 + 0.032 * 0.8 = 0.0896$
- $l' = 0.064 + 0.032 * 0.6 = 0.0832$
- $r' = h' - l' = 0.0896 - 0.0832 = 0.0064$



\$

$$h' = l + r * \max$$
$$l' = l + r * \min$$

- $h = 0.0896$
 - $l = 0.0832$
 - $r = 0.0064$
 - $h' = 0.0832 + 0.0064 * 1 = 0.08960$
 - $l' = 0.0832 + 0.0064 * 0.8 = 0.08832$
 - Answer:
- Any number within the range
 ~ 0.08832
- Simplest decimal within the
 0.089

