

Triangular Arbitrage

1. Doug Bernard specializes in cross-rate arbitrage. He notices the following quotes:

Swiss franc/U.S dollar = SFr 1.5971/\$

Australian dollar/U.S. dollar = A\$ 1.8215/\$

Australian dollar/Swiss franc = A\$ 1.1440/SFr

- Ignoring transaction costs, does Doug Bernard have an arbitrage opportunity based on these quotes?
- If there is an arbitrage opportunity, what steps would he take to make an arbitrage profit, and how would he profit if he has \$1,000,000 available for this purpose.

Answer

A.

The implicit cross-rate between Australian dollars and Swiss franc is $A\$/SFr = A\$/\$ \times \$/SFr = (A\$/\$)/(\$/SFr) = 1.8215/1.5971 = 1.1405$. However, the quoted cross-rate is higher at A\$1.1440/SFr.

So, triangular arbitrage is possible.

B.

In the quoted cross-rate of A\$1.1440/SFr, one Swiss franc is worth A\$1.1440, whereas the cross-rate based on the direct rates implies that one Swiss franc is worth A\$1.1405. Thus, the Swiss franc is overvalued relative to the A\$ in the quoted cross-rate, and Doug Bernard's strategy for triangular arbitrage should be based on selling Swiss francs to buy A\$ as per the quoted cross-rate. Accordingly, the steps Doug Bernard would take for an arbitrage profit is as follows:

- i. Sell dollars to get Swiss francs: Sell \$1,000,000 to get $\$1,000,000 \times \text{SFr}1.5971/\$ = \text{SFr}1,597,100$.
- ii. Sell Swiss francs to buy Australian dollars: Sell SFr1,597,100 to buy $\text{SFr}1,597,100 \times \text{A}\$1.1440/\text{SFr} = \text{A}\$1,827,082.40$.
- iii. Sell Australian dollars for dollars: Sell A\$1,827,082.40 for $\text{A}\$1,827,082.40/\text{A}\$1.8215/\$ = \$1,003,064.73$.

Thus, your arbitrage profit is $\$1,003,064.73 - \$1,000,000 = \$3,064.73$.

2. Assume you are a trader with Deutsche Bank. From the quote screen on your computer terminal, you notice that Dresdner Bank is quoting $\text{€}0.7627/\$1.00$ and Credit Suisse is offering $\text{SF}1.1806/\$1.00$. You learn that UBS is making a direct market between the Swiss franc and the euro, with a current €SF quote of $.6395$. Show how you can make a triangular arbitrage profit by trading at these prices. (Ignore bid-ask spreads for this problem.) Assume you have $\$5,000,000$ with which to conduct the arbitrage.

What happens if you initially sell dollars for Swiss francs? What €SF price will eliminate triangular arbitrage?

Answer

To make a triangular arbitrage profit the Deutsche Bank trader would sell $\$5,000,000$ to Dresdner Bank at $\text{€}0.7627/\$1.00$. This trade would yield $\text{€}3,813,500 = \$5,000,000 \times .7627$. The Deutsche Bank trader would then sell the euros for Swiss francs to Union Bank of Switzerland at a price of $\text{€}0.6395/\text{SF}1.00$, yielding $\text{SF}5,963,253 = \text{€}3,813,500/.6395$. The Deutsche Bank trader will resell the Swiss francs to Credit Suisse for $\$5,051,036 = \text{SF}5,963,253/1.1806$, yielding a triangular arbitrage profit of $\$51,036$. If the Deutsche Bank trader initially sold $\$5,000,000$ for Swiss francs, instead of euros, the trade

would yield $SF5,903,000 = \$5,000,000 \times 1.1806$. The Swiss francs would in turn be traded for euros to UBS for $\text{€}3,774,969 = SF5,903,000 \times .6395$. The euros would be resold to Dresdner Bank for $\$4,949,481 = \text{€}3,774,969 / .7627$, or a loss of $\$50,519$. Thus, it is necessary to conduct the triangular arbitrage in the correct order.

The $S(\text{€}/SF)$ cross exchange rate should be $.7627/1.1806 = .6460$. This is an equilibrium rate at which a triangular arbitrage profit will not exist. (The student can determine this for himself.) A profit results from the triangular arbitrage when dollars are first sold for euros because Swiss francs are purchased for euros at too low a rate in comparison to the equilibrium cross-rate, i.e., Swiss francs are purchased for only $\text{€}0.6395/SF1.00$ instead of the no-arbitrage rate of $\text{€}0.6460/SF1.00$. Similarly, when dollars are first sold for Swiss francs, an arbitrage loss results because Swiss francs are sold for euros at too low a rate, resulting in too few euros. That is, each Swiss franc is sold for $\text{€}0.6395/SF1.00$ instead of the higher no-arbitrage rate of $\text{€}0.6460/SF1.00$.

3. Suppose we have the following data:

$i_{JPY} = 1\%$ for 1 year ($T=1$ year)

$i_{BRL} = 10\%$ for 1 year ($T=1$ year)

$S = .025$ BRL/JPY

We construct the following strategy, called *carry trade*, to “profit” from the interest rate differential:

Today, at time $t=0$, we do the following (1)-(3) transactions:

- (i) Borrow JPY 1,000 at 1% for 1 year. (At $T=1$ year, we will need to repay JPY 1,010.)
- (ii) Convert to BRL at $S = .025$ BRL/JPY. Get BRL 25.
- (iii) Deposit BRL 25 at 10% for 1 year. (At $T=1$ year, we will receive BRL 27.50.)

Now, we *wait* 1 year. At time $T=1$ year, we do the final step:

- (iv) Exchange BRL 27.50 for JPY at ST

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If $S_{t+T} = .022$ BRL/JPY, we will receive JPY 1250, for a profit of JPY 240.

- If $S_{t+T} = .025$ BRL/JPY, we will receive JPY 1100, for a profit of JPY 90.

- If $S_{t+T} = .027$ BRL/JPY, we will receive JPY 1019, for a profit of JPY 9.

- If $S_{t+T} = .030$ BRL/JPY, we will receive JPY 916, for a profit of JPY -74.