## Comparative Advantage and the Gains from International Trade

Thematic Area 2

## MSc in ISFM

## Trade occurs because of:

- Differences across countries in endowments of labour, physical capital, natural resources, and technology
- Economies of scale (larger scale of production is more efficient)
- The Ricardian model focuses on differences in the productivity of labour (due to differences in technology) between countries.

The Ricardian Model demonstrates that it is possible for a country to gain from international trade even if it is less productive than foreign countries in the production of all goods.

To demonstrate this we rely on the concepts of:

- absolute advantage, and
- comparative advantage.

We explain these concepts with the aid of a simple example...

## Main Assumptions of the Model

- 2 Countries: Denmark(D) and Greece (G)
- 2 Goods: Agricultural (A) and Manufacturing (M)
- Labour is the only factor of production, and all workers are identical within each country.
- Labour productivity varies across countries (possibly due to differences in technology).
- Labour productivity remains constant as output changes.
- The supply of labor in each country is constant.
- Perfect competition prevails in all markets.

The Table below shows the units of labour required to produce 1 unit of each good in each country. Thus, for example, to produce 1 unit of $M$ in Greece (G) you need 4 units of labour, whereas in Denmark (D) you need 1 unit of labour. We observe that, for both goods, you need fewer units of labour in $D$ than in $G$. We thus say that $D$ has absolute advantage in the production of both goods over $G$ (i.e. $D$ it is more productive in both goods). However, the productivity advantage of $D$ (over G ) is four times as high in M , and "only" twice as high in A. Thus, D has comparative advantage in $M$. By same token, although $G$ has absolute disadvantage in both goods, it has comparative advantage in A (in A, Greece has $50 \%$ of Danish productivity, and in M, 25\% of Danish productivity - thus Greece is comparatively better in A).

LABOUR UNITS REQUIRED TO PRODUCE 1 UNIT OF THE GOOD

AGRICULTURAL GOODS (A)
MANUFACTURING GOODS (M)

GREECE (G)
DENMARK (D)

2
1 1

## Relative Prices in Autarky

Assuming perfect competition, the price of each good in autarky will be equal to the average cost of producing it. Thus:

$$
\begin{aligned}
& P^{A, G}=A C^{A, G}=2\left(W^{G}\right) \\
& P^{M, G}=A C^{M, G}=4\left(W^{G}\right) .
\end{aligned}
$$

Therefore the relative price in Greece in autarky will be equal to :
$\left(P^{A, G} / P^{M, G}\right)=0.5$. This makes sense, since it takes half as much labour to produce the A good in Greece as the amount required to produce the M good.
Applying the same logic, the relative price in Denmark in autarky will be equal to: $\left(P^{A, D} / P^{M, D}\right)=1$. NOTE: UNDER AUTARKY, THE RELATIVE PRICE OF GOOD A IS LOWER IN GREECE - COMPARATIVE ADVANTAGE (CA) IMPLIES THAT UNDER AUTARKY THE RELATIVE PRICE OF THE GOOD IN WHICH THE COUNTRY HAS CA WILL BE LOWER THAN IN THE OTHER COUNTRY. (GOOD M WILL BE RELATIVELY CHEAP IN DENMARK.)

## Real Wages in Autarky (1)

Workers within each country are identical, and earn the same wage.

Under autarky, the real wage in terms of A in Greece will be $W^{G} / P^{A, G}=W^{G} / 2\left(W^{G}\right)=0.5$.

This implies that a worker can acquire half a unit of $A$ if he provides 1 unit of labour and devotes his entire income to acquire the A good; in other words, real wages are equal to labour productivity, since 1 unit of labour produces half a unit of $A$.

The real wage in terms of M goods in Greece will be $W^{G} / P^{M, G}=W^{G} / 4\left(W^{G}\right)=0.25$. (This implies that a worker can acquire 0.25 units of M if he provides 1 unit of labour and devotes his entire income to acquire the M good.)

## Real Wages in Autarky (2)

By similar reasoning, the real wage in Denmark will be:

$$
\begin{array}{rll}
W^{D} / P^{A, D}=W^{D} / W^{D}=1 & \text { - in terms of } \mathrm{A} \\
W^{D} / P^{M, D}=W^{D} / W^{D}=1 & \text { - in terms of M }
\end{array}
$$

Real wages will be higher in the more productive country.

## A Hypothetical Consumption Pattern in Autarky

- Given that in autarky in Greece
$W^{G} / P^{A, G}=0.5$, and $W^{G} / P^{M, G}=0.25$, a worker could, for example, find it optimal to devote half her income (from supplying 1 unit of labour) to buy 0.25 units of $A$, and the other half to buy 0.125 units of M . We denote this as:
$C_{a}{ }^{A, G}=0.25, \quad C_{a}{ }^{M, G}=0.125$. (subscript $a$ denotes autarky)
- Given that in autarky in Denmark
$W^{D} / P^{A, D}=1$, and $W^{D} / P^{M, D}=1$, a worker could, for example, may prefer to devote $80 \%$ of her income (from supplying 1 unit of labour) to buy 0.8 units of $M$ and the rest $20 \%$ to buy 0.2 units of $A$. We denote this as:
$C_{a}^{A, D}=0.2, \quad C_{a}^{M, D}=0.8$

Consumption Pattern in Autarky:
Under Autarky, point $\alpha$ (in both diagrams) is the production and consumption point, since consumption of each good can not differ from the production of each good in the absence of international trade.



## Free Trade

- Under autarky we found that that the relative prices will be different in the two countries: $\left(P^{A, G} / P^{M, G}\right)=0.5$, $\left(P^{A, D} / P^{M, D}\right)=1$.
- Free trade (and the absence of any regulations or taxes) will equalize the prices, and a common relative price will prevail, denoted as $\left(P^{A} / P^{M}\right)$.
- We expect that free trade will result in a relative price that will be in-between the autarkic relative prices, i.e. $0.5<\left(P^{A} / P^{M}\right)<1$. (The case that the relative price under free trade will be equal to either 0.5 or 1 cannot a-priori be excluded, but we ignore it here.)
- For purposes of illustration, let's assume that the freetrade relative price is: $\left(P^{A} / P^{M}\right)=0.8$.


## Are There Gains from Trade?

- With free trade it makes sense for each country to specialize in producing only the good in which it has comparative advantage (i.e., G in A, and D in M). For simplicity, assume that there is only 1 worker in each country, who supplies 1 unit of labour.
- Suppose that the Greek worker, who produces 0.5 units of A, wishes to maintain her consumption of 0.25 units of $A$ (as in autarky), and trade (i.e. export) her remaining 0.25 units of A in order to acquire, thru imports, some units of $M$.
- How many units of imports can she receive in exchange?
- Since the value of imports must be equal to the value of exports, i.e.
$\left(P^{A}\right)\left(X^{A}\right)=\left(P^{M}\right)\left(I M^{M}\right)$, or $I M^{M}=\left(P^{A} / P^{M}\right)\left(X^{A}\right)$,
where $X$ denotes exports, and IM denotes imports. Since $X^{A}=0.25$, and $\left(P^{A} / P^{M}\right)=0.8$, we find that $I M^{M}=0.2$


## Are There Gains from Trade (continued)

- Thus, the worker can, thru trade, maintain her consumption of 0.25 units of $A$, and consume 0.20 units of $M$ as well, which are higher than the consumption of 0.125 units of $M$ which she would have in autarky.
- In such a case, since Greece's exports of A are 0.25 units, Denmark's imports of A will be 0.25 units, and that will be the Danish worker's consumption of $A$, which is higher than his consumption under autarky (=0.2). Moreover, since the Danish worker produces 1 unit of $M$, and exports 0.20 units of it to Greece, his consumption of M would be 0.80 units - as much as her consumption during autarky.
- This case is depicted for both countries in the next slide, with $\alpha$ depicting the production and consumption point under autarky, and $Q$ and $C$ the production and consumption points (respectively) under free trade.

Gains from Trade: In the example presented, for both countries, free trade allows them, by fully specializing in the good in which they have CA, to consume as much of the good in which they have CA, and to increase the consumption of the other good thru imports. This obtains because world production of both goods rises under free trade relative to autarky.



## Gains from Trade (continued)

- Of course, the worker could enjoy, thru free trade, higher consumption of both goods relative to autarky.
- For example, the worker in Greece could consume 0.28 units of A, export 0.22 units of it, and import and consume 0.176 units of $M-$ since $\left(P^{A} / P^{M}\right)\left(X^{A}\right)=(0.8)(0.22)=0.176$ (which is higher than 0.125 which would have in autarky).
- In that case, the consumption of the Danish worker will be equal to $0.5-0.28=0.22$ units of $A$ (instead of 0.2 in autarky), and 1-0.176=0.824 units of the $M$ good (instead of 0.8 ).
- The fact that workers can enjoy higher consumption of both goods under free trade relative to autarky signifies Gains from Trade.


## Relative Wages

- Given the productivity differences between the two countries, how high could the Greek wage be relative to the Danish wage ( $W^{G} / W^{D}$ )?
- It is obvious that the Greek wage should be such that Greece can produce at least one of the goods at a lower cost - otherwise, with free trade, no Greek producer could survive.
- We need $A C^{A, G} \leq A C^{A, D}$, or (2) $W^{G} \leq W^{G}$, or $\left(W^{G} / W^{D}\right) \leq 1 / 2$. This says that the Greek wage can be, at most, $50 \%$ of the Danish wage. Why? Because Greek workers have $50 \%$ of the productivity of Danish workers.
- How low could $\left(W^{G} / W^{D}\right)$ be? By similar logic we can establish that if ( $W^{G} / W^{D}$ ) <1/4, then even M could be produced in G at a lower cost than in D. Thus...


## Relative Wages (continued)

- Thus, the relationship:

$$
1 / 4 \leq\left(W^{G} / W^{D}\right) \leq 1 / 2
$$

provides the range of the Greek wage relative to the Danish wage that allows both countries to produce at least one of the goods.

- For example, if $W^{G}=0.4, W^{D}=1$, then $A C^{A, G}<A C^{A, D}$, and $A C^{M, G}>A C^{M, D}$, so $G$ will produce the $A$, and $D$ the $M$.
- The relative demand for the two goods determines whether $W^{G} / W^{D}$ should be closer to the lower or the higher value of the range (i.e. closer to 0.25 or to 0.5 ). For example, an exogenous increase in the (relative) demand for A will result in higher demand for labour in Greece, and a higher $W^{G} / W^{D}$.


## Changes in Foreign Productivity

- We have seen that in autarky real wages are equal to (labour) productivity, and that with free trade the real wage in terms of the imported good will be higher. Moreover, the rise in the real wage (and consumption possibilities) for Greece after free trade obtains even if the trading partner ( $\mathbf{D}$ ) is more productive in both goods.
- What if, starting from a situation of free trade, D becomes more productive? Will Greece become better-off?
- Consider that D's productivity in agricultural goods rises, and that it now requires only 0.666 units of labour to produce 1 unit of $A$.
- Greece retains its CA in $A$, since it has $33 \%$ of D's productivity in it, and only $25 \%$ of D's productivity in M. Thus, Greece can continue to specialize in producing the $A$.
- The range of the Greek wage relative to the Danish wage now is $1 / 4 \leq\left(W^{G} / W^{D}\right) \leq 1 / 3$; i.e. Greek wages can now be up to $33 \%$ of Danish ones.
- Although we may care about relative wages (e.g. Harvard survey), what happens to real wages?
- If, as assumed earlier, $\left(W^{G} / W^{D}\right)=0.4$ before the rise in D's productivity, assume that after the rise in D's productivity $\left(W^{G} / W^{D}\right)=0.3$. Let $W^{D}=1$, in both cases, so that $W^{G}=0.4$, and $W^{G}=0.3$, respectively.
- Note that the price of each good under free trade is equal to the AC of producing, and that with full specialization $G$ produces $A$ and $D$ produces M.
- Then it is easy to establish that the real wage with respect to the A good will be the same in Greece (before and after the change in D's productivity), but the real wage with respect to the M good will become lower.
- This example illustrates that it is possible for a country to lose from changes in foreign productivity. Does it also imply that the country may become worse-off relative to autarky? NO.

