

Ειδικά Θέματα Αλγορίθμων  
Ασκήσεις Φροντιστηρίου #5  
Average Case and Probabilistic Analysis

**1. Hiring Problem:** A set of  $n$  candidates will be interviewed sequentially, each interview incurs cost  $c_i$  (small), each hire incurs cost  $c_h$  (large), to hire a new candidate we have to fire the one we hired previously.

**Goal:** Hire the best candidate

Find the average-case total cost for the above problem.

**2. Secretary Problem:** A set of  $n$  candidates will be interviewed sequentially, but this time once a candidate is hired the process stops.

**Goal:** Hire the best candidate

What is the optimal strategy to maximize our chances of selecting the top candidate?

**3.** How many people must there be in a room before there is a 50% chance that two of them were born on the same day of the year?