

1) a) 0-6m

$$60 + 30 - 100 - 30 = -40$$

$$b) \sqrt{\left\{ 60 \times 0.02 + 40 \times 0.10 + 30 \times (0.025 + 0.017) \right.}$$

$$\left. - 100 - (0.01) - 30(0.025 + 0.0075) \right\}$$

$$\sqrt{(-40) \times (-0.0030)}$$

c) $90 \times 10\% = 9$ run off

$$c \rightarrow a: -40 + 9 = -31$$

$$c \rightarrow b: -31 \times (-0.0030)$$

2) a)
$$D = \left\{ -1 \frac{9}{1.09} - 2 \frac{9}{1.09^2} - 3 \frac{9}{1.09^3} - 4 \frac{9}{1.09^4} - 5 \frac{99}{1.09^5} \right\} / P$$

$$P = \frac{9}{1.09} + \frac{9}{1.09^2} + \frac{9}{1.09^3} + \frac{9}{1.09^4} + \frac{109}{1.09^5}$$

b)
$$\Delta P = P \times \frac{D}{1.09} - (0.0030)$$

3) a) $V_{\alpha R} = \alpha \times \sigma(R_P) \times W$, $\alpha = 2.33$, $W = 1 \text{ mil } \text{€}$

$$\sigma(R_P) = \left\{ 0.40^2 \times (0.012)^2 + 0.60^2 \times (0.007)^2 + 2 \times 0.40 \times 0.60 \times 0.8 \times (0.012) \times (0.007) \right\}^{1/2}$$

b) $CV_{\alpha R_B} = (0.60) \times b_B \times V_{\alpha R}$

$$b_B = \frac{\text{cov}(R_B, W_A R_A + W_B R_B)}{\sigma^2(R_P)} = \frac{W_A \text{cov}(R_A, R_B) + W_B \sigma^2(R_B)}{\sigma^2(R_P)}$$

where: $\text{cov}(R_A, R_B) = 0.8 \times (0.012) \times (0.007)$

$$4) A: \frac{25}{\sqrt{5} \times 1.65} = 6.77$$

$$B: \frac{17}{\sqrt{3} \times 2.33} = 4.21$$

$$C: \frac{36}{\sqrt{5} \times 1.96} = 4.74$$

$$D: \frac{32}{\sqrt{2} \times 2.33} = 3.96$$

$$5) P(1 + 0.047) + (1-P)(1 + 0.047)(0.30) = 1 + 0.013$$

$$\Rightarrow P(1 + 0.047)(1 - 0.30) = 1.013 - (1 + 0.047)(0.30)$$

$\Rightarrow P =$ probability of repayment \Rightarrow

$1-P =$ " " default

6) ~~99%~~ one-side with a normal distribution $\rightarrow a = 2.33$

we notice that: $120 \times 2.33 \times 0.0715 = 20$ mil €

if s.d. $(R) = 0.12$ then

$$120 \times 2.33 \times 0.12 = 33.55 \text{ mil €}$$

The F.I. has a probability of suffering losses equal to:
 $0.05 \times 0.01 = 0.0005$ (0.05%)

So the collateral should increase to:

$$\text{Collateral} \times (1 - 2.33 \times 0.12) = 100 \Rightarrow$$

$$\text{Col} = \frac{100}{0.7204} = 138.81 \text{ mil €}$$

7) Capital required by the regulations on capital adequacy: $10 \text{ mil} \times 0.5 \times 0.08 = 0.4 \text{ mil } \text{€}$

$$0.15 = \frac{\{(X - 0.015) + 0.003\} \times 10 \text{ mil } \text{€}}{0.4 \text{ mil}}$$

\Rightarrow Solve for X.

8) Tier I ^{required} regulatory capital:

$$\left[\begin{array}{l} 80 \times 0.2 + 120 \times 0.5 + 240 \times 1 \\ (40 \times 1 + 80 \times 0.2) \times 0.5 \end{array} \right] \times 0.06 = 20.64$$

if what you find from above is ~~15~~ 15 mil €
then the FR is not adequately capitalized

The difference is the deficit in Tier I capital